

Start recording!

Physics 2A: Lecture 2

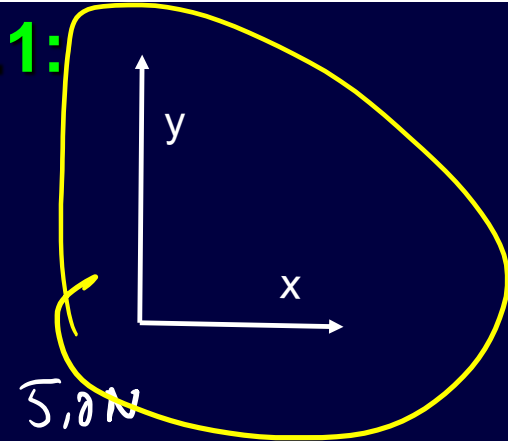
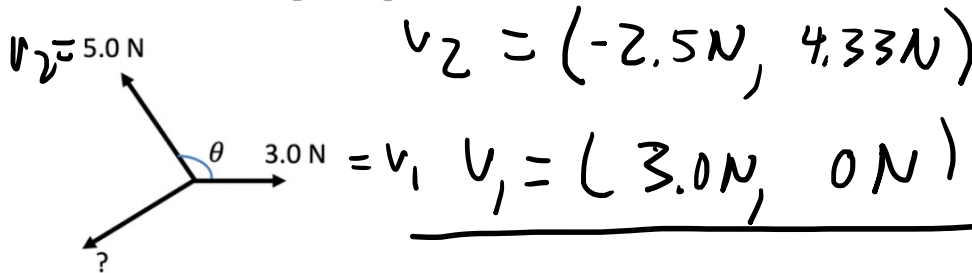
Today's Agenda

- The study of motion
 - Describing motion
 - Example from last week
- Kinematics
 - Position
 - Velocity
 - Acceleration
- Special case: Constant acceleration

Clicker Question 0.1:

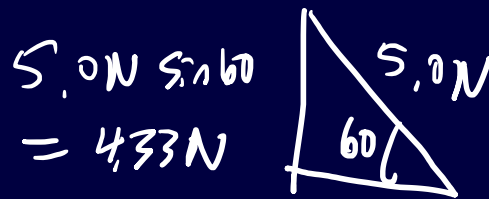
Question 3

The figure below shows a birds-eye-view of three people pulling on ropes that are connected together at a single point. One person pulls with a force of 3.0 N and a second person pulls with a force of 5.0 N at angle of $\theta = 120$ degrees from the first person, as in the figure. With what magnitude of force must the third person pull with such that the three forces cancel out?



What is the y-component of the 5.0 N vector? Assume our usual xy-axis as shown.

- (a) 4.33 N
- (b) -4.33 N
- (c) 2.5 N
- (d) -2.5 N



Handwritten calculation:

$$5.0\text{ N} \cos 60 = 2.5\text{ N}$$



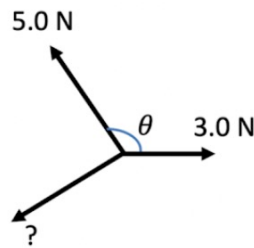
Handwritten result for the vector components:

$$\vec{v}_2 = (-2.5\text{ N}, 4.33\text{ N})$$

Clicker Question 0.2:

Question 3

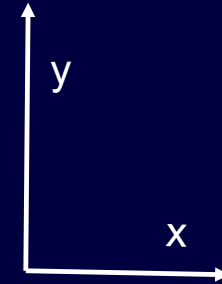
The figure below shows a birds-eye-view of three people pulling on ropes that are connected together at a single point. One person pulls with a force of 3.0 N and a second person pulls with a force of 5.0 N at angle of $\theta = 120$ degrees from the first person, as in the figure. With what magnitude of force must the third person pull with such that the three forces cancel out?



$$V_1 = (3.0 \text{ N}, 0 \text{ N})$$

$$V_2 = (-2.5 \text{ N}, 4.33 \text{ N})$$

$$V_{TOT} = (0.5 \text{ N}, 4.33 \text{ N})$$

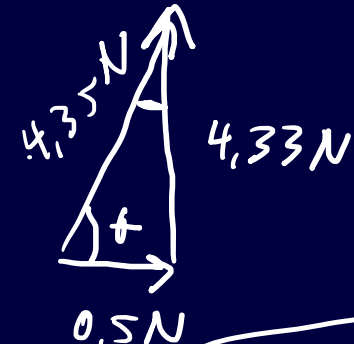


What angle does the vector sum of the 3.0 N and 5.0 N vector make with the x-axis?

- (a) 6.6 degrees
- (b) 12.6 degrees
- (c) 35.2 degrees
- (d) 59.1 degrees
- ☒ (e) 83.4 degrees

$$\tan \theta = \frac{0}{A} = \frac{4.33}{0.5}$$

$$\theta = \tan^{-1} \left[\frac{4.33}{0.5} \right] = 83.4^\circ$$

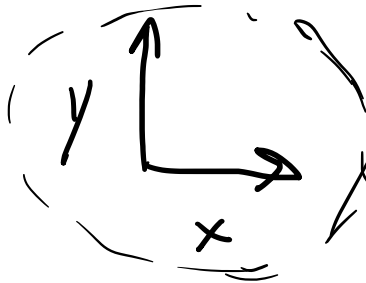
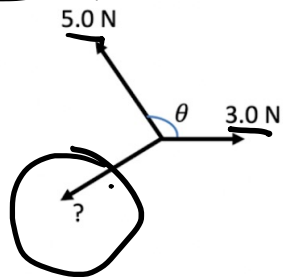


$$H = \sqrt{0.5 \text{ N}^2 + 4.33 \text{ N}^2} = 4.35 \text{ N}$$

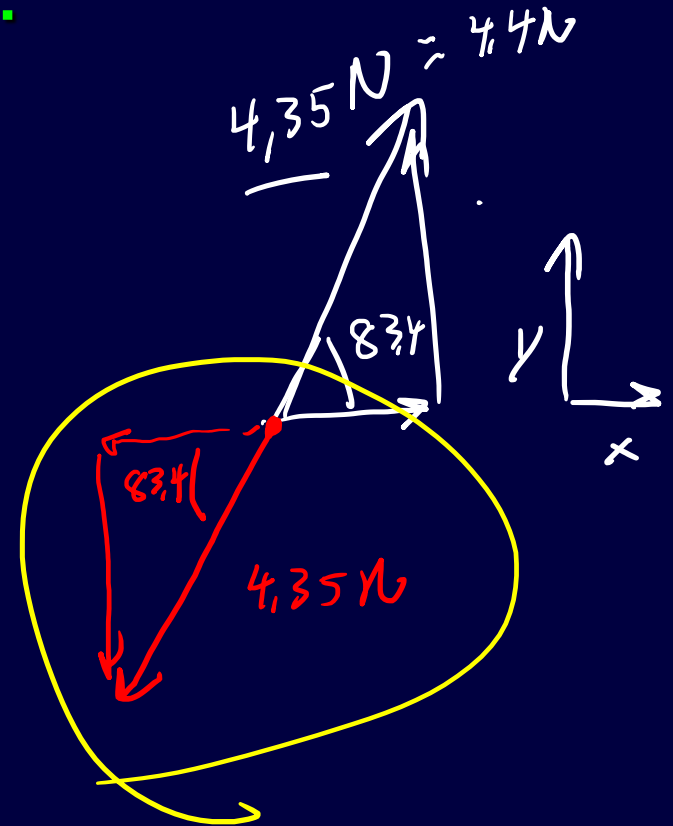
Clicker Question 0:

Question 3

The figure below shows a birds-eye-view of three people pulling on ropes that are connected together at a single point. One person pulls with a force of 3.0 N and a second person pulls with a force of 5.0 N at angle of $\theta = 120$ degrees from the first person, as in the figure. With what magnitude of force must the third person pull with such that the three forces cancel out?



- (A) 2.5 N (B) 7.0 N (C) 2.8 N. (D) 4.4 N. (E) 5.2 N. (F) 6.3 N



Clicker Question 2:

A box rests on an incline. The force of gravity pulls straight down as shown. When dealing with inclined planes we will often find it convenient to rotate our coordinate system as shown. How would you express the gravitational force in the new x-direction?

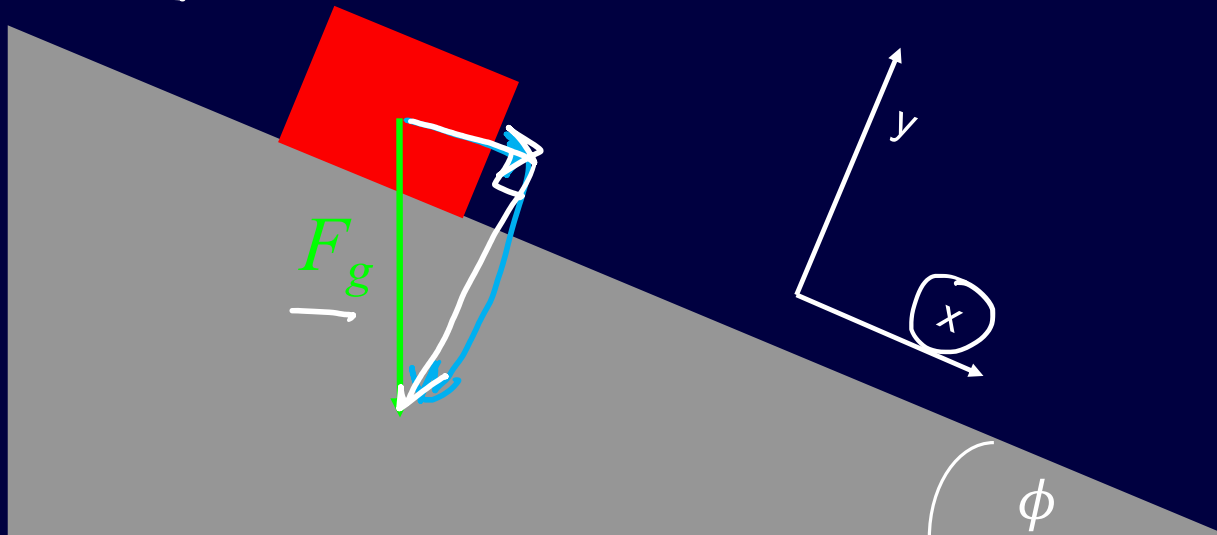
(a) $F_g \cos(\phi)$

(b) $F_g \sin(\phi)$

(c) ~~$-F_g \cos(\phi)$~~

(d) ~~$-F_g \sin(\phi)$~~

(e) None of the above



Example: Inclined surface

+ pos

$$(F_g)_x = +F_g \sin A = F_g \sin(\phi)$$

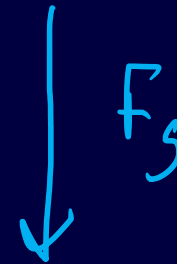
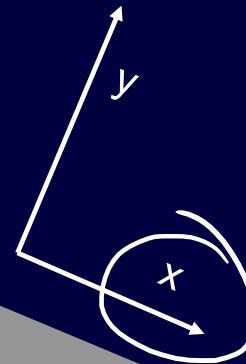
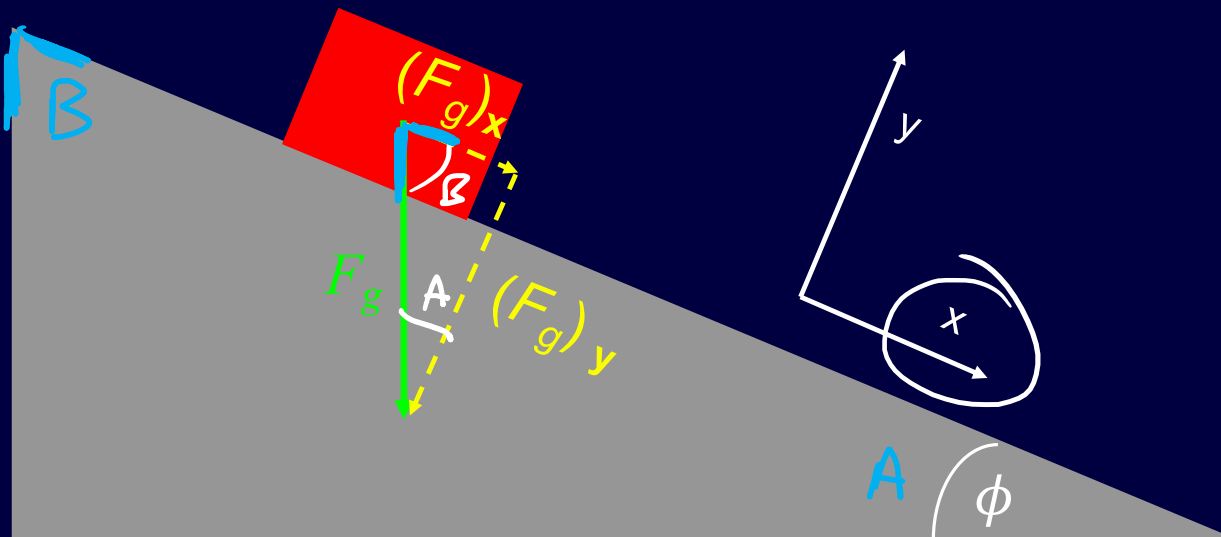
$$(F_g)_y = -F_g \cos A = -F_g \cos \phi$$



$2P_B^4$

$1P_B^3$

In pos y-direction!



Speed and velocity

- How fast is the object changing position?

$$\text{speed} = |\vec{v}|$$

$$\text{speed}_{\text{ave}} = |\vec{v}_{\text{ave}}| = \frac{\text{distance}}{\text{time}}$$

- Speed is only a magnitude, how fast an object moves
- **Instantaneous speed:** Speed at an instant in time.
- Velocity is a vector, speed and direction

Acceleration

- Acceleration: Change in velocity over time **(It's a vector)**
- Average acceleration = change in velocity / elapsed time

$$\vec{a}_{\text{ave}} = \frac{\Delta \vec{v}}{\Delta t} = \frac{\vec{v}_f - \vec{v}_i}{t_f - t_i}$$

- **Instantaneous acceleration:** Acceleration at an exact instant in time
- Units = meters per second per second = m/s² ←
- For velocity and acceleration we'll drop the instantaneous from now on

Units of acceleration

- Think about as m/s per second (It's like the speed of the velocity)

$$a = \frac{\frac{m}{s}}{s} = \frac{m}{s^2}$$

Acceleration

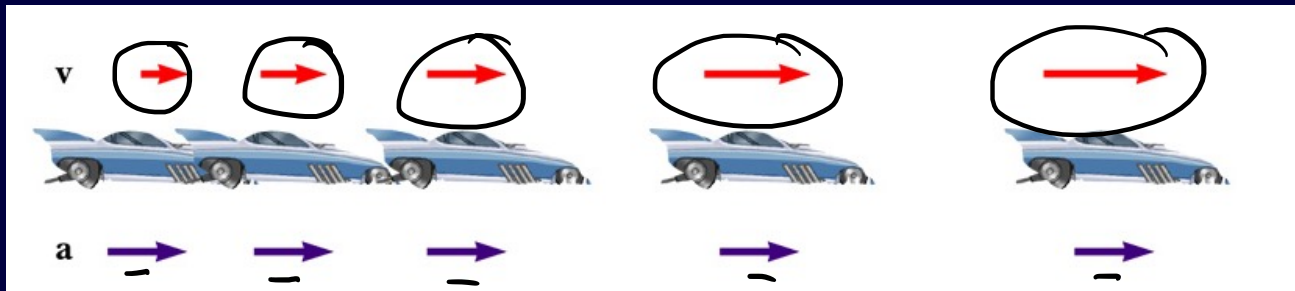
- Assume we start at rest with acceleration of 5 m/s^2
- At time = 1s we have velocity 5 m/s
- At time = 2s we have velocity 10 m/s
- At time = 3s we have velocity 15 m/s

Object is speeding up, or accelerating!

And its doing it at a constant rate!

Relationship Between Velocity and Acceleration

$a = \text{constant}$, \uparrow



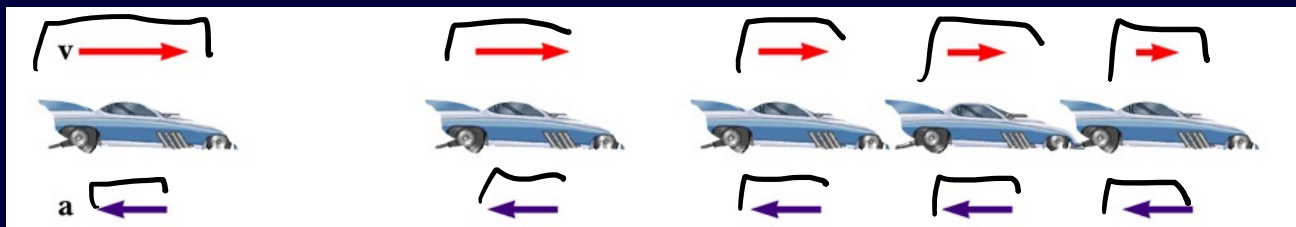
- Velocity and acceleration are in the same direction
- Acceleration is uniform (blue arrows maintain the same length)
- Velocity is increasing (red arrows are getting longer)
- Positive velocity and positive acceleration

Relationship Between Acceleration and Velocity



- Uniform velocity (shown by red arrows maintaining the same size)
- Acceleration equals zero

Relationship Between Velocity and Acceleration



- Acceleration and velocity are in opposite directions
- Acceleration is uniform (blue arrows maintain the same length)
- Velocity is decreasing (red arrows are getting shorter)
- Velocity is positive and acceleration is negative

Clicker Question 3:

A ball is thrown vertically upward. At the very top of its trajectory, which of the following statements is true:

- (a) The velocity of the ball is zero and the acceleration of the ball is zero
- (b) The velocity of the ball is not zero and the acceleration of the ball is zero
- (c) The velocity of the ball is zero and the acceleration of the ball is not zero
- (d) The velocity of the ball is not zero and the acceleration of the ball is not zero

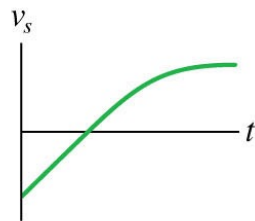
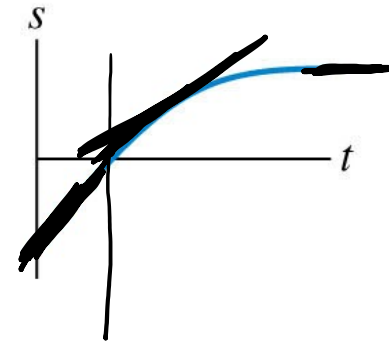
Instantaneous Velocity

- Objects rarely travel for long with a constant velocity.
- Far more common is a velocity that changes with time.
- If you watch a car's speedometer, at any instant of time, the speedometer tells you how fast the car is going *at that instant*.
- If we include directional information, we can define an object's **instantaneous velocity**—speed and direction—as its velocity at a single instant of time.
- The average velocity $v_{\text{avg}} = \Delta s / \Delta t$ becomes a better and better approximation to the instantaneous velocity as Δt gets smaller and smaller.

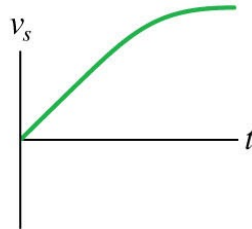
$$v_s \equiv \lim_{\Delta t \rightarrow 0} \frac{\Delta s}{\Delta t} = \frac{ds}{dt} \quad (\text{instantaneous velocity})$$

Clicker Question 4:

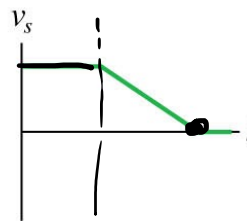
Which velocity-versus-time graph goes with this position graph?



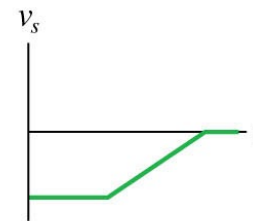
(a)



(b)



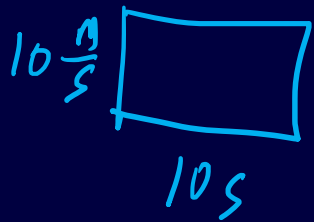
(c)



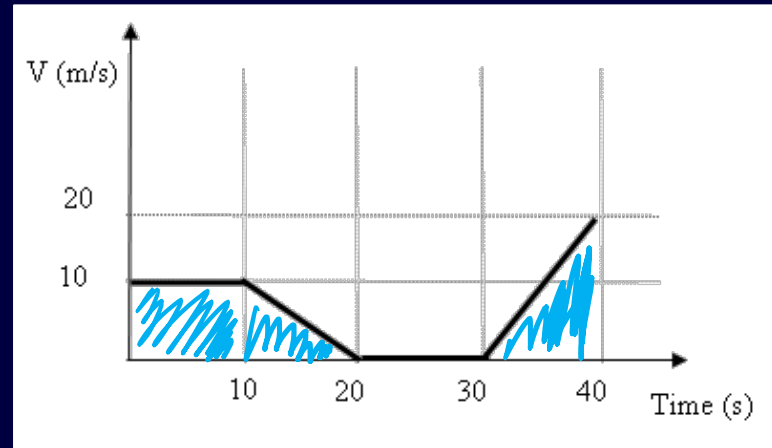
(d)

Clicker Question 4.5:

Below is a v vs. t graph for a car. What was the displacement of the car between $t = 0$ s and $t = 40$ s ?

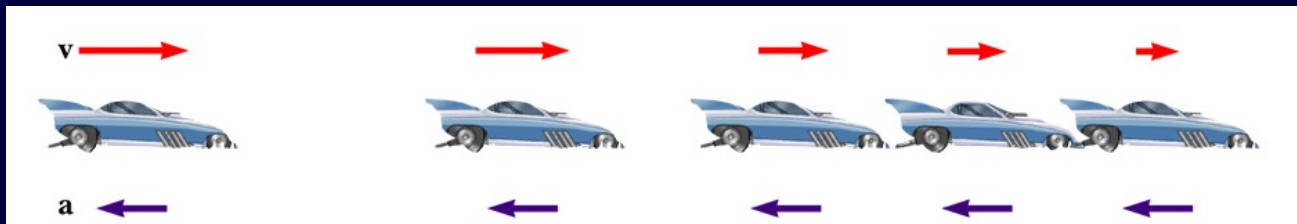
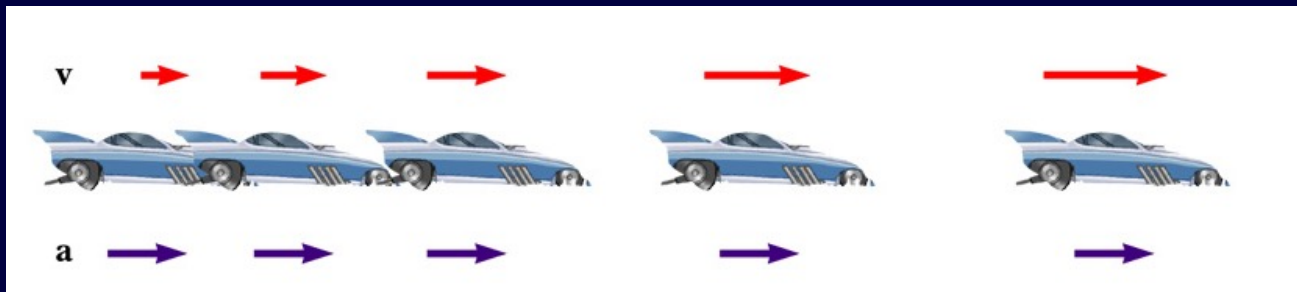


- (a) 0 m
- (b) 200 m
- (c) 250 m
- (d) 350 m
- (e) 550 m



$$\text{one box} = \left(10 \frac{m}{s}\right) 10s$$
$$= 100 \text{ m}$$

$$1 \quad 0.5 \quad 1 = 2.5 \text{ box}$$



Where to get help

- Lectures (podcast posted the afternoon of each lecture)
- Discussions (LAs will offer extra sections if requested)
- Office hours
 - Andrew: Tuesday and Thursday from 2-3pm ✓
 - Wanda: Wednesday and Thursday 4-5pm ✓
 - Raj: Wednesday and Thursday 9-10am ✓
 - Sharath: ✓
- Supplemental Instruction
 - Erica Yang
 - Wednesdays and Thursdays 11-12:20
 - <https://ucsd.zoom.us/j/92155353023>
- PIAZZA

The Constant Acceleration Model

$$\rightarrow v_F = v_0 + at \quad \rightarrow t$$

$$\rightarrow x_F = x_0 + v_0 t + \frac{1}{2} at^2 \quad \rightarrow$$

$$\underline{g = 9.81 \text{ m/s}^2}$$

These can be combined to make:

$$\boxed{v_F^2 = v_0^2 + 2a(\Delta x)}$$

$$\underline{-g = -9.81 \text{ m/s}^2}$$

Student: I am confused about whether or not when should i use negative 9.81 for gravity and when should I use 9.81 for gravity?

Student: How do you know which equation to use, whether it's the velocity and position equations or the combined one?

Constant Acceleration Equations

$$v_F = v_0 + at$$

$$y_F = y_0 + v_0 t + \frac{1}{2} at^2$$

$$v_F^2 = v_0^2 + 2a(\Delta y)$$

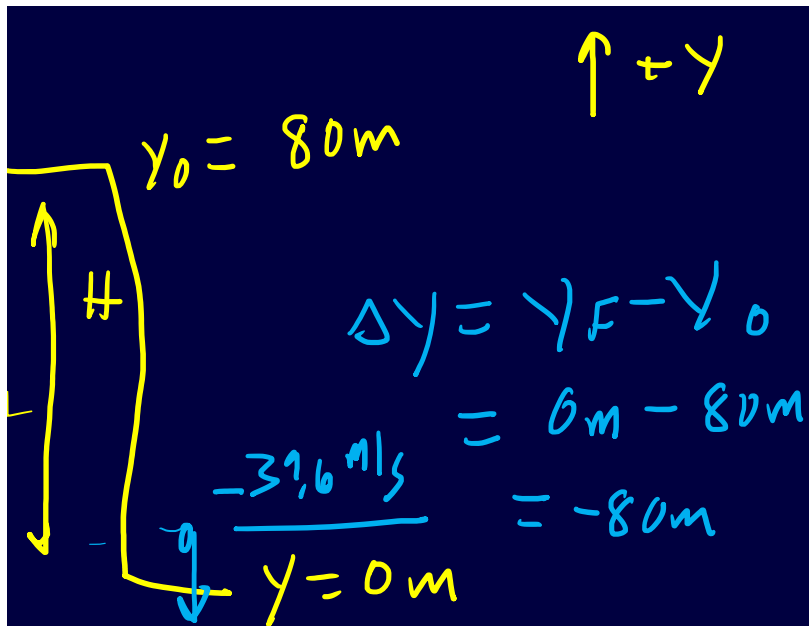
Same equations but in the up and down direction.

Clicker Question 5:

I **drop** a ball off a cliff of height 80 m. ✓ How long will it take the ball to reach the ground? What **speed** will it have right before it hits the ground? ✓

- (a) $t = 2.35 \text{ s}$, $v_F = 23.0 \text{ m/s}$
- (b) $t = 9.81 \text{ s}$, $v_F = 56.2 \text{ m/s}$
- (c) $t = 5.34 \text{ s}$, $v_F = 52.4 \text{ m/s}$
- (d) $t = 4.03 \text{ s}$, $v_F = 39.6 \text{ m/s}$
- (e) $t = 2.45 \text{ s}$, $v_F = 24.0 \text{ m/s}$

Student: Shouldn't the answer for problem 2 be -39.6 instead of positive because it is a downward velocity



$$a_y = -g = -9,81\text{m/s}^2$$

$$y_0 = 80\text{m},$$

$$y_F = 0\text{m},$$

$$v_0 = 0$$

$$y_F = y_0 + v_0 t^0 + \frac{1}{2} a t^2$$

$$0 = 80\text{m} - \frac{1}{2} g t^2$$

$$\frac{1}{2} g t^2 = 80\text{m}$$

$$t^2 = \frac{2(80\text{m})}{g}$$

$$t = \sqrt{\frac{2(80\text{m})}{g}}$$

$$= 4,03\text{s}$$

$$v_F = v_0 + a t$$

$$= -g t$$

$$= -(9,81\text{m/s}^2) \times (4,03\text{s})$$

$$= -39,6\text{m/s}$$

$$v_F^2 = v_0^2 + 2 a \Delta y$$

$$= -2g(-80\text{m})$$

$$v_F = \pm \sqrt{2g(80\text{m})}$$