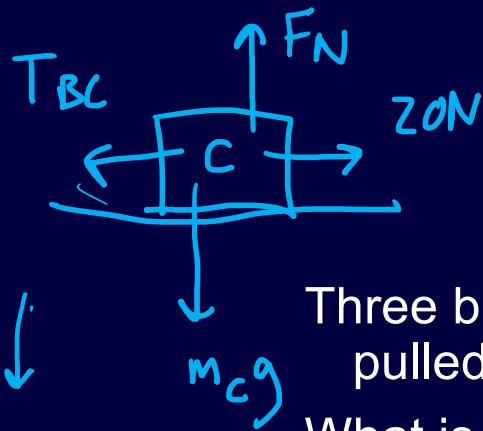


# Physics 2A: Lecture 6

## Today's Agenda

- Uniform Circular Motion
- Centripetal acceleration
- Examples
  - Car on track
  - Carnival ride
  - Loop-de-loop

**Start Recording!**



### Conceptual Problem 5:

Three blocks each have a mass of 3 kg and are being pulled over a frictionless surface by a force of 20 N.

What is the tension between blocks B and C,  $T_{BC}$ ?

$$a = 2.22 \text{ m/s}^2$$

$$\sum F_x = m a_x$$

$$20 \text{ N} - T_{BC} = m_c a$$

$$-T_{BC} = m_c a - 20 \text{ N}$$

A 1

B 2

C 3

**D 4**

E 5

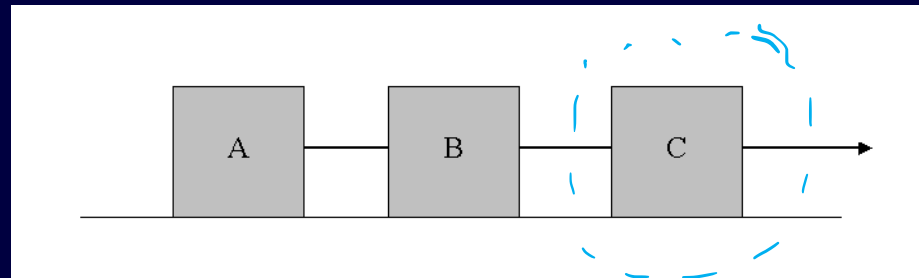
a) 3.32 N

b) 6.67 N

c) 13.34 N

d) 20 N

e) 26.7 N



$$-1 \left[ -T_{BC} = m_c a - 20 \text{ N} \right]$$

$$T_{BC} = 20 \text{ N} - m_c a = 13.34 \text{ N}$$

Three blocks each have a mass of 3 kg and are being pulled over a frictionless surface by a force of 20 N.

What is the tension between blocks B and C?

A)

B)

C)

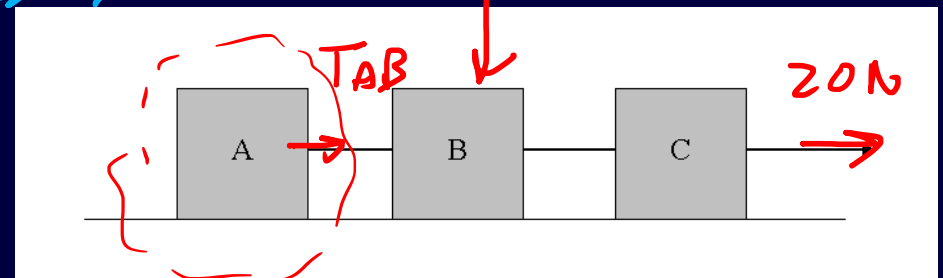
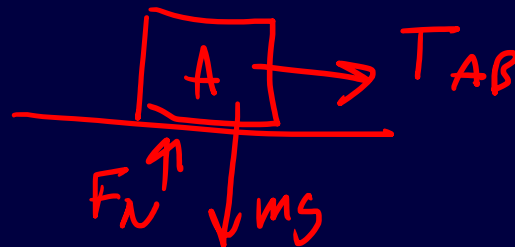
A) 3.32 N

B) 6.67 N

C) 13.34 N

D) 20 N

A B  $T_{AB}$



$$\sum F_x = m_A a$$

$$T_{AB} = (3 \text{ kg}) (2.22 \text{ m/s}^2)$$

$$= \underline{6.67 \text{ N}}$$

## Example

pulleys  
massless

$$\sum F_y = m_8 a_y = 0$$

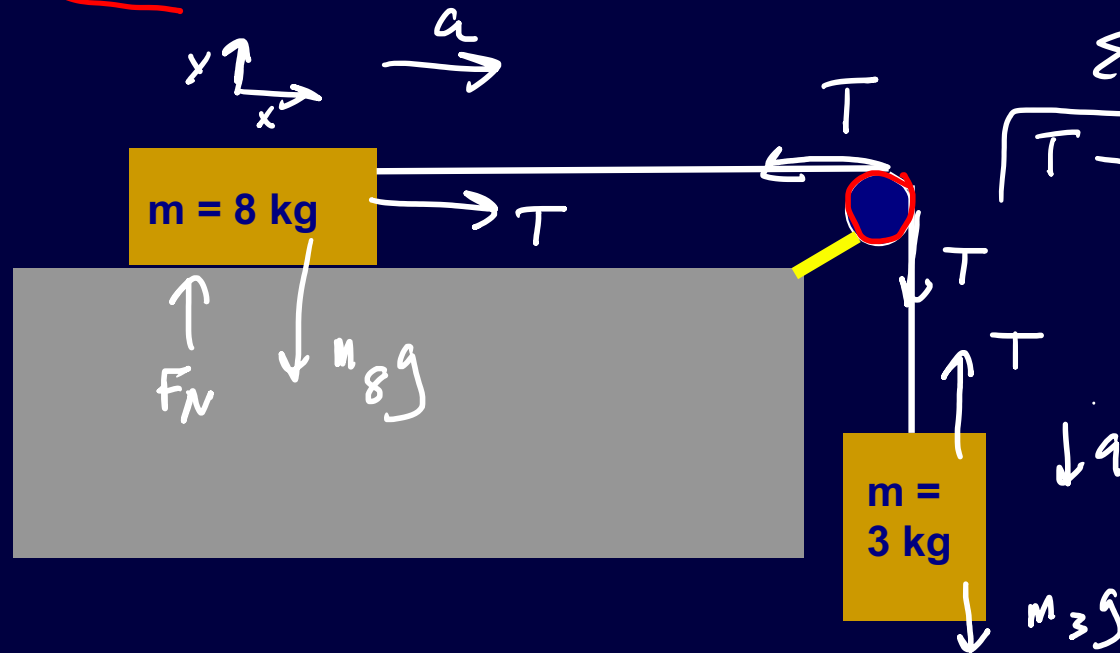
- Assume two blocks are set up as below. There is no friction between the top block and the table. What is the acceleration of the blocks?

$$F_N - m_8 g = 0$$

$$F_N = m_8 g$$

$$\sum F_x = m_8 a_x$$

$$T = m_8 a$$

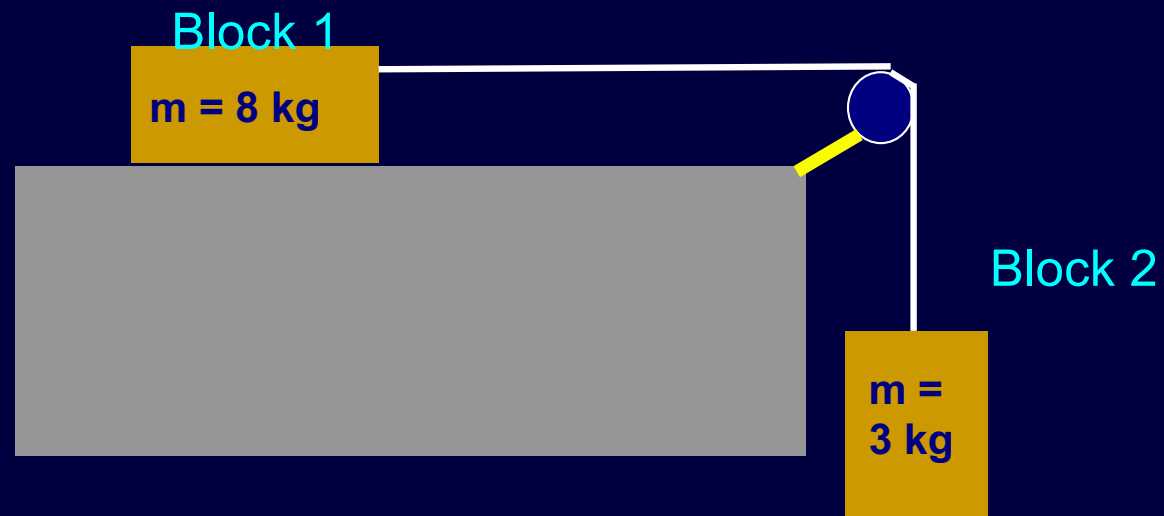


$$\sum F_y = m_3 a_y$$

$$T - m_3 g = -m_3 a$$

## Example

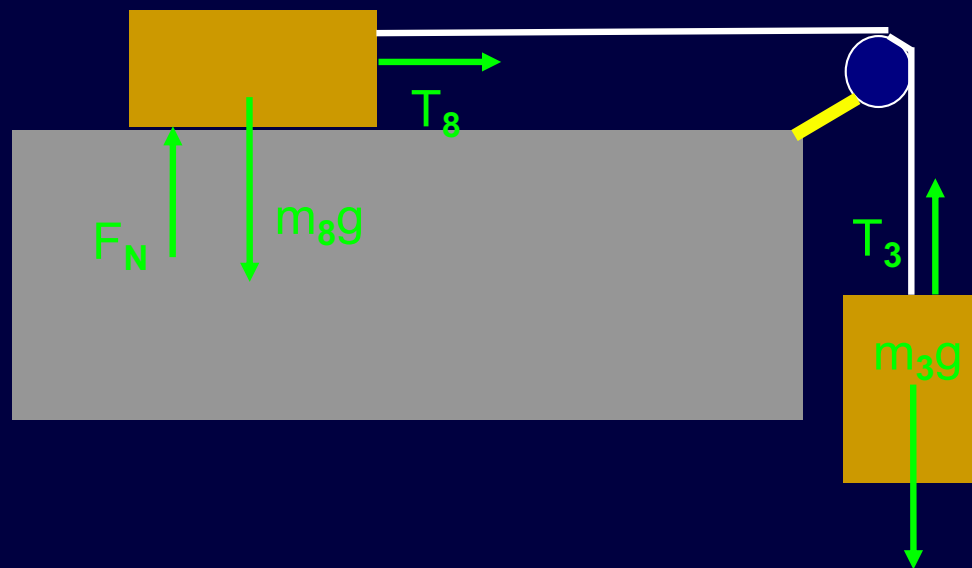
- Step 1: Select the objects of interest.
- The two blocks, must work with both of them.



## Example

- Step 2: Draw a Free Body Diagram

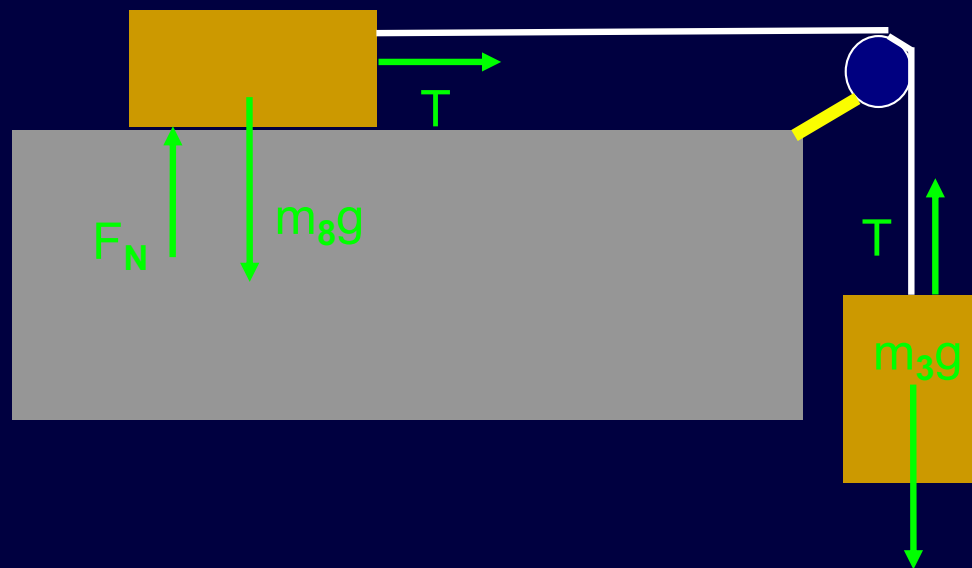
- 1.) Weight due to gravity
  - 2.) Normal Force on block 1
  - 3.) Tensions
- What Forces act on the blocks?



**Acceleration constraint!**

## Example

Step 5: Apply Newton's Second law.





$$a = ?$$

## Example

Step 5: Apply Newton's Second law.

$$T = m_8 a$$

$$T - m_3 g = -m_3 a$$

$$m_8 a - m_3 g = -m_3 a$$

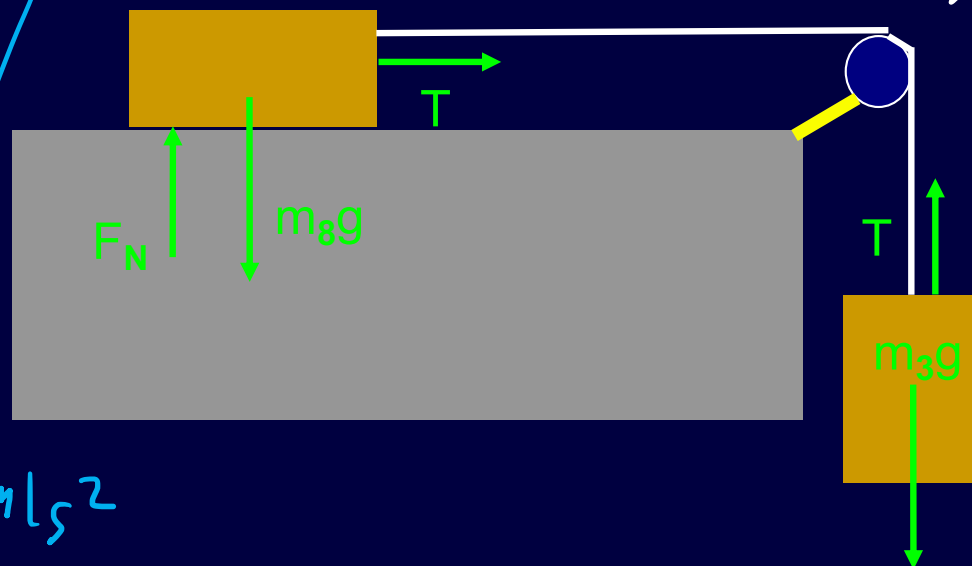
$$m_8 a + m_3 a = m_3 g$$

$$a(m_8 + m_3) = m_3 g$$

$$a = \frac{m_3 g}{m_8 + m_3} = 2.67 \text{ m/s}^2$$

$$ma = \sum F$$

$$a$$



- a)  $1.33 \text{ m/s}^2$
- b)  $3.14 \text{ m/s}^2$
- c)  $2.67 \text{ m/s}^2$
- d)  $5.13 \text{ m/s}^2$
- e)  $1.78 \text{ m/s}^2$

$$a = 2.67 \text{ m/s}^2$$

## Clicker Question 6:

Assume two blocks are set up as below. There is no friction between the top block and the table. What is the tension in the rope?

- a) 8.0 N
- b) 13.4 N
- c) 21.4 N
- d) 29.37 N
- e) 33.33 N



$$T = m_8 a = 8 \text{ kg} (2.67 \text{ m/s}^2) = 21.4 \text{ N}$$

$$T - m_3 g = -m_3 a$$

$$T = m_3 g - m_3 a = 21.4 \text{ N}$$

## Clicker Question 1:

Bob pushes on a cart of mass 50 kg with a horizontal force  $F_{push}$ . There is no friction. The cart has an acceleration of  $5 \text{ m/s}^2$ .

Which one of the following statements is true?

- (a) By Newton's third law, the cart applies an equal and opposite force of magnitude  $F_{push}$  on Bob.
- (b) The cart applies an opposite force on Bob, but it is smaller in magnitude than  $F_{push}$  because of the acceleration force.
- (c) The force the cart applies on Bob is responsible for the acceleration of the cart.
- (d) The cart applies no force on Bob, because it is not pushing back on him.
- (e) The cart applies an opposite force on Bob and it is larger in magnitude than  $F_{push}$ .

**Student:** If the answer to problem 1 is A, I don't really understand how the cart can accelerate positively if the net force in the horizontal direction is zero. Or maybe the net force in the horizontal direction is not equal to zero and I'm missing why the horizontal net force is not equal to zero?

## Clicker Question 1:

**Student:** If the answer to problem 1 is A , I don't really understand how the cart can accelerate positively if the net force in the horizontal direction is zero. Or maybe the net force in the horizontal direction is not equal to zero and I'm missing why the horizontal net force is not equal to zero?



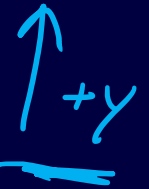
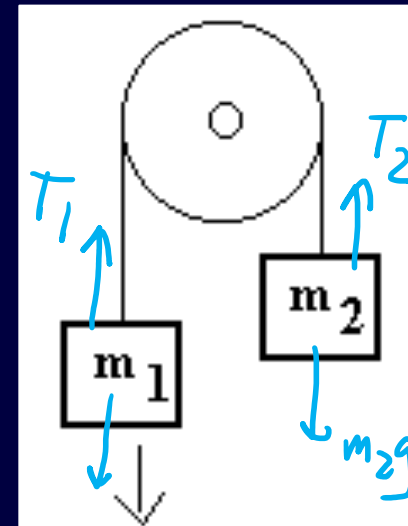
## Clicker Question 2:

Two blocks,  $m_1 = 5 \text{ kg}$  and  $m_2 = 3 \text{ kg}$ , are connected by a massless rope around a frictionless pulley as pictured below. Which equation below would be a result of applying Newton's second law correctly to either block 1 or block 2? Call the tension acting on block 1  $T_1$  and the tension acting on block 2  $T_2$ .

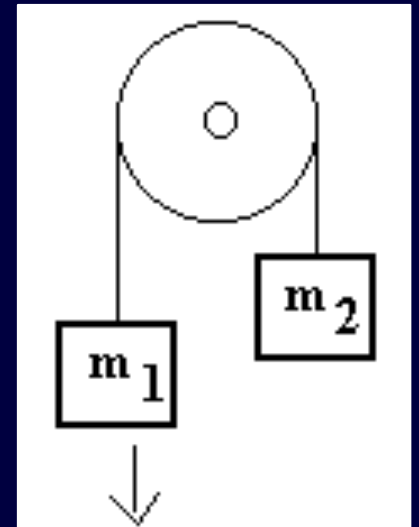
- ~~(A)~~  $T_1 - m_1 g = m_1 a_1$   
 (B)  $-T_1 - m_1 g = -m_1 a_1$   
 (C)  $-T_1 + m_1 g = +m_1 a_1$   
 (D)  $-T_2 + m_2 g = -m_1 a_2$   
 (E)  $T_2 - m_2 g = -m_2 a_2$

$$\begin{aligned}
 m_1 \downarrow \quad \Sigma F &= m_1 a \\
 (T_1 - m_1 g) &= -m_1 a \\
 \hline
 -T_1 + m_1 g &= m_1 a
 \end{aligned}$$

$$\begin{aligned}
 m_2 \downarrow \quad \Sigma F &= m_2 a \quad g \downarrow \\
 \hline
 T_2 - m_2 g &= m_2 a
 \end{aligned}$$



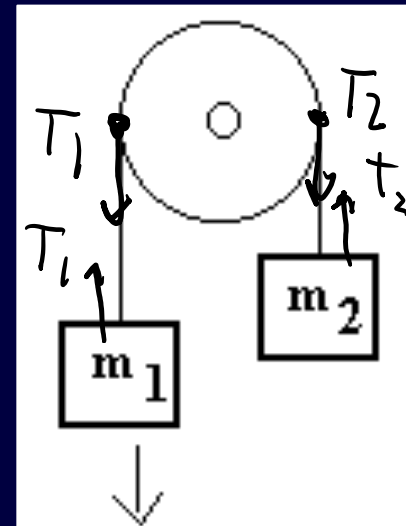
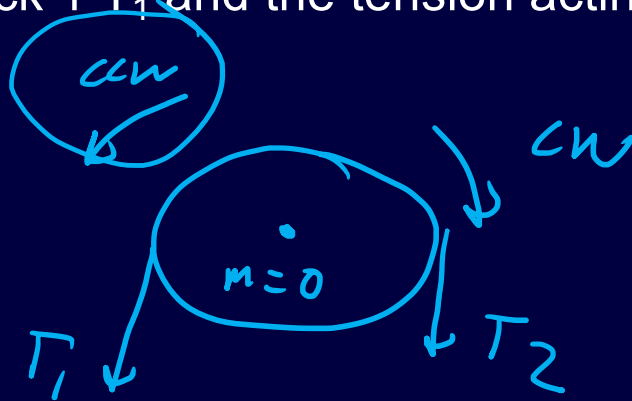
Two blocks,  $m_1 = 5 \text{ kg}$  and  $m_2 = 3 \text{ kg}$ , are connected by a massless rope around a frictionless, massless pulley as pictured below. Which equation below would be a result of applying Newton's second law correctly to either block 1 or block 2? Call the tension acting on block 1  $T_1$  and the tension acting on block 2  $T_2$ .



### Clicker Question 3:

Two blocks,  $m_1 = 5 \text{ kg}$  and  $m_2 = 3 \text{ kg}$ , are connected by a massless rope around a frictionless, massless pulley as pictured below. Call the tension acting on block 1  $T_1$  and the tension acting on block 2  $T_2$ . Which statement is correct?

- (A)  $T_1 > T_2$
- (B)  $T_1 = T_2$
- (C)  $T_1 < T_2$



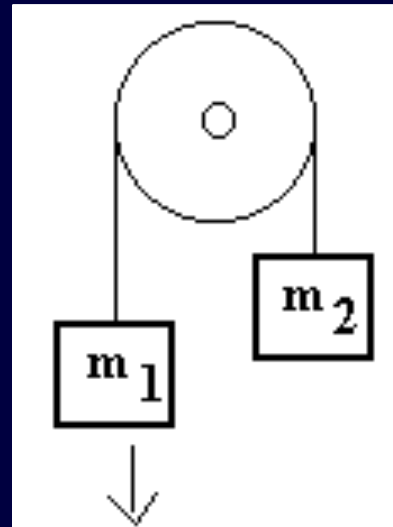
### Clicker Question 4:

$a = \text{same}$

Two blocks,  $m_1 = 5 \text{ kg}$  and  $m_2 = 3 \text{ kg}$ , are connected by a rope around a frictionless, massless pulley as pictured below. What is the acceleration of block 1?

- a)  $18.0 \text{ m/s}^2$
- b)  $8.19 \text{ m/s}^2$
- c)  $3.90 \text{ m/s}^2$
- d)  $2.45 \text{ m/s}^2$
- e)  $1.17 \text{ m/s}^2$

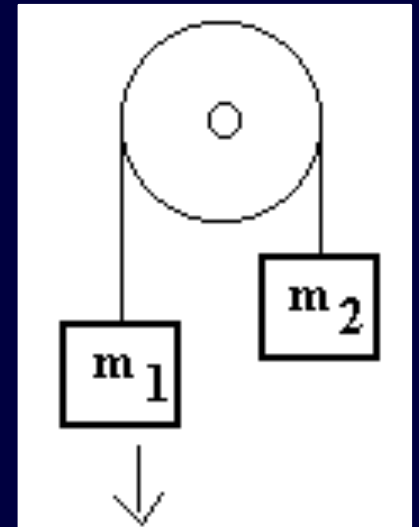
$$a = \frac{m_1 g - m_2 g}{m_1 + m_2} =$$



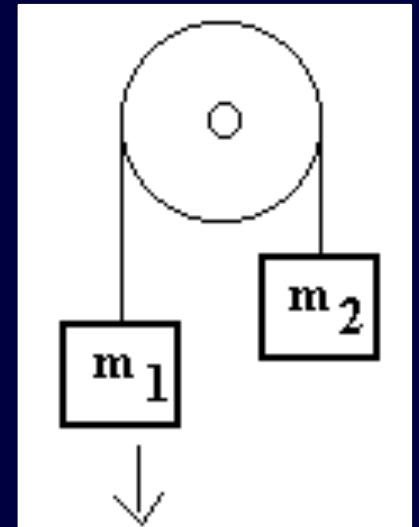
$$\begin{aligned} T - m_1 g &= -m_1 a \\ T - m_2 g &= m_2 a \\ \hline T &= m_2 a + m_2 g \\ m_2 a + m_2 g - m_1 g &= -m_1 a \\ (m_1 a + m_2 a) &= m_1 g - m_2 g \end{aligned}$$



Two blocks,  $m_1 = 5 \text{ kg}$  and  $m_2 = 3 \text{ kg}$ , are connected by a massless rope around a frictionless pulley as pictured below. What is the acceleration of block 1?



Two blocks,  $m_1 = 5 \text{ kg}$  and  $m_2 = 3 \text{ kg}$ , are connected by a massless rope around a frictionless, massless pulley as pictured below. What is the acceleration of block 1?



$$\underline{\Sigma F = ma}$$

### Clicker Question 5:

$$m_1 > m_2$$

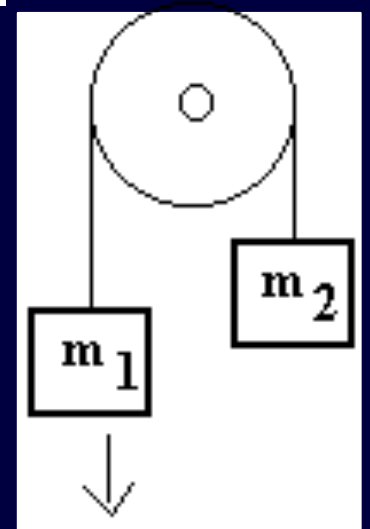
Two blocks,  $m_1 = 5 \text{ kg}$  and  $m_2 = 3 \text{ kg}$ , are connected by a rope around a frictionless, massless pulley as pictured below. Which statement is true about the magnitude of the net force on  $m_2$ ?

- (a) It's greater than the magnitude of the net force on  $m_1$ .
- (b) It's equal to the magnitude of the net force on  $m_1$ .
- (c) It's less than the magnitude of the net force on  $m_1$ .

$$m_1 a > m_2 a$$

$$T - m_1 g$$

$$T - m_2 g$$

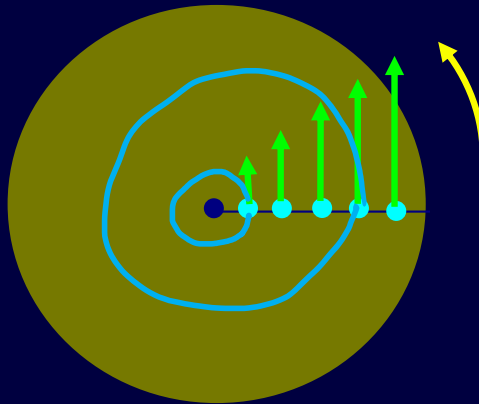


# Rotational motion



- When dealing with a rotating object our 'old-fashioned' variables come up short.
  - Every point goes a different distance
  - Every point has a different speed and accel.

Outside points must go faster to make one revolution in same amount of time!

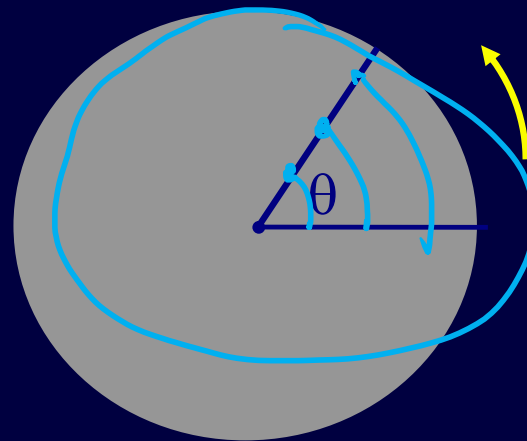
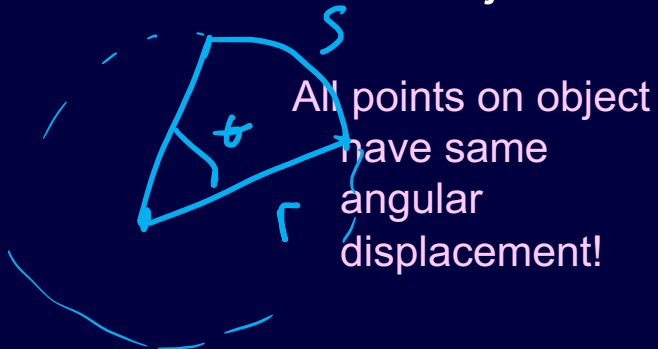


$$\theta = \frac{s}{r}$$

## Angular Displacement

$$\theta = \frac{2\pi r}{r} = \underline{2\pi}$$

- Angular Displacement: Angle through which an object rotates about a fixed axis

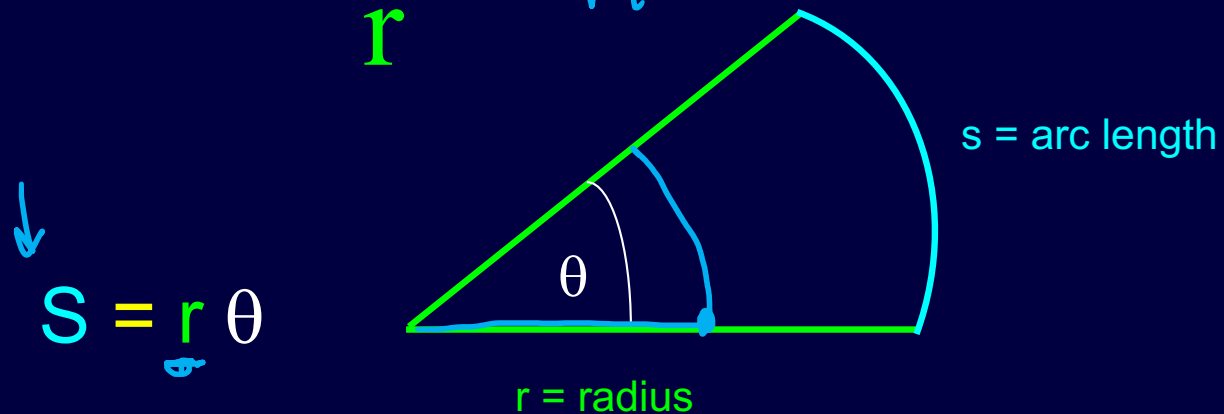


We draw a line and observe the angle the line moves through.

- $\Delta\theta = \theta_f - \theta_i$  (usually measured in radians)
- Positive if counterclockwise; Negative if clockwise

## Definition of radians

$$\theta = \frac{s}{r} = \frac{m}{m} \Rightarrow \underline{\text{Unitless}}$$



Bigger radius more arc length with same angle!!

## Angular Velocity

- **Angular Velocity**: How fast an object rotates.
- Denoted with Greek letter  $\omega$  **omega**

$$\boxed{\omega_{av}} = \frac{\Delta\theta}{\Delta t} = \frac{\theta_f - \theta_i}{t_f - t_i} \quad \frac{\text{rad}}{\text{s}}$$

- Units (radian/s)      **Analog of linear velocity**
- **Positive** if counterclockwise; **Negative** if clockwise

## Tangential vs. angular

- Tangential distance vs. angular distance

$$\boxed{s = \theta R}$$

- Tangential velocity vs. angular velocity

$$\boxed{v_T = \omega R}$$

- Tangential acceleration vs. angular acceleration

$$\boxed{a_T = \alpha R}$$

- Angular values are same for all points, tangential are not!!!

$$s = \theta R$$

$$\frac{ds}{dt} = \frac{d\theta}{dt} R$$

$$\underline{v} = \underline{\omega} R$$



## The 'viewer' equation

- We can start with this equation and develop an equation to relate angular velocity and tangential velocity

$$s = \theta r$$

$$\frac{s}{t} = \frac{\theta}{t} r$$

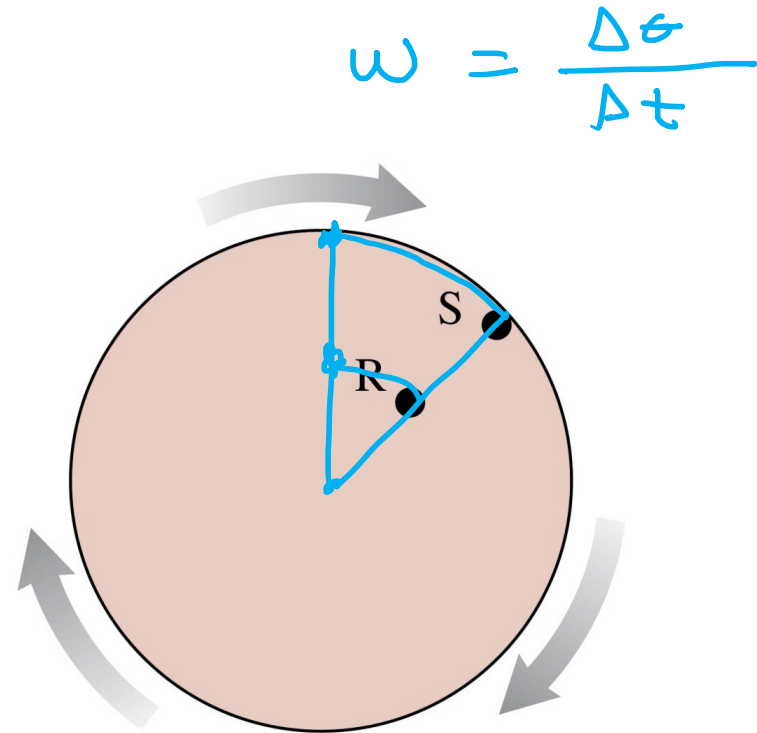
$$V_T = \omega r$$

- Tangential values are larger the farther out the radius  $r$  is

## Clicker 6:

Rasheed and Sofia are riding a merry-go-round that is spinning steadily. Sofia is twice as far from the axis as is Rasheed. Sofia's angular velocity is \_\_\_\_\_ that of Rasheed.

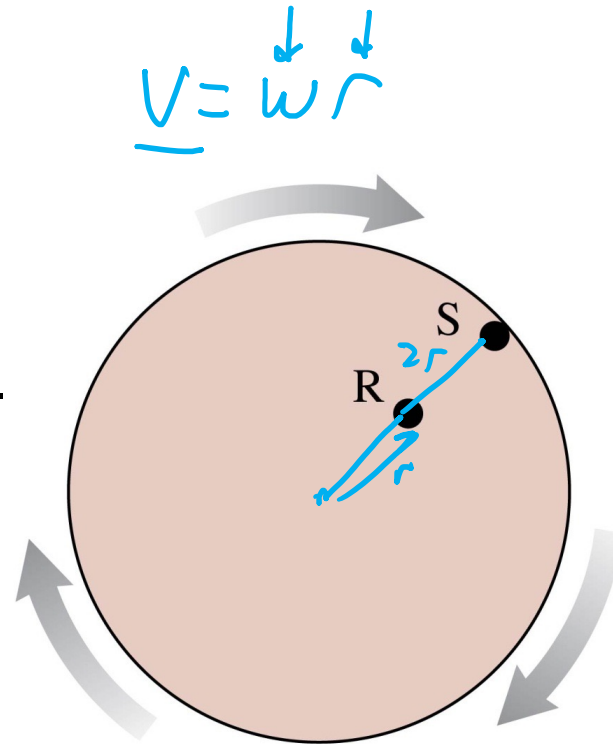
- A. half
- B. the same as
- C. twice
- D. four times
- E. We can't say without knowing their radii.



## Clicker 7:

Rasheed and Sofia are riding a merry-go-round that is spinning steadily. Sofia is twice as far from the axis as is Rasheed. Sofia's speed is \_\_\_\_\_ that of Rasheed.

- A. half
- B. the same as
- C. twice
- D. four times
- E. We can't say without knowing their radii.



# Equations of Rotational Kinematics

- Equations of Rotational Kinematics

- $\theta_F = \omega_0 t + \frac{1}{2}\alpha t^2$

- $\omega_F = \omega_0 + \alpha t$

- $\omega_F^2 = \omega_0^2 + 2\alpha\Delta\theta$

- Only good when  $\alpha$  is constant

- Use in a similar manner as the linear equations

### Clicker Question 8:

A rotor in a car's brake system has an angular velocity of 50 rad/s. By applying the brakes the brake pads produce an angular acceleration of  $15 \text{ rad/s}^2$ . How many turns will the rotor make in the meantime?

(a) 13.26 rev

(b) 83.33 rev *e*

(c) 24.56 rev

(d) 18.79 rev

(e) 34.78 rev

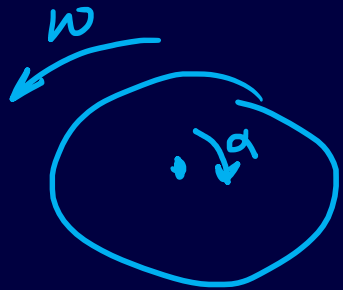
$$83.33 \text{ rad}$$

$$N = \frac{83.33 \text{ rad}}{2\pi \frac{\text{rev}}{\text{rad}}} = \underline{13.26 \text{ rev}}$$

A rotor in a car's brake system has an angular velocity of 50 rad/s. By applying the brakes the brake pads produce an angular acceleration of 15 rad/s<sup>2</sup>. How many turns will the rotor make in the meantime?

$$\omega_0 = 50 \frac{\text{rad}}{\text{s}}$$

$$\alpha = -15 \frac{\text{rad}}{\text{s}^2}$$



$$\downarrow \omega_F^2 = \downarrow \omega_0^2 + 2 \downarrow \alpha (\Delta \theta)$$

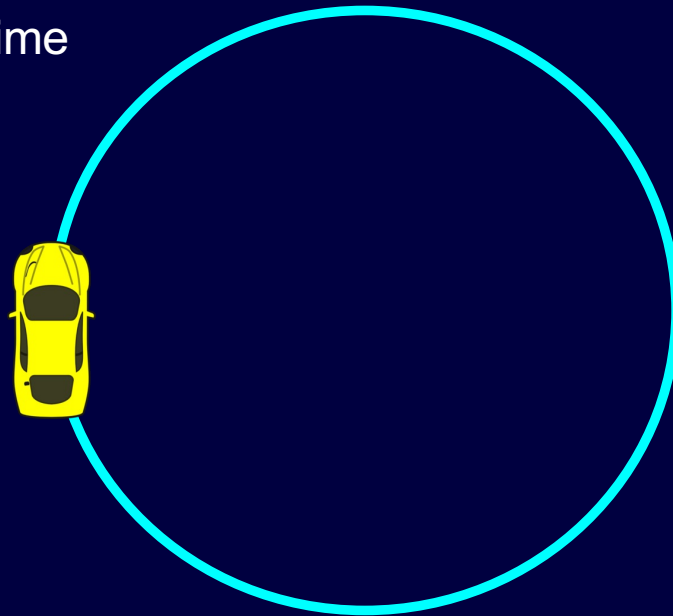
$$0 = \omega_0^2 + 2 \alpha \Delta \theta$$

$$\Delta \theta = \frac{\omega_0^2}{-2\alpha} = \frac{(50 \text{ rad/s})^2}{2 (15 \frac{\text{rad}}{\text{s}^2})} = \underline{83.33 \text{ rad}}$$

## Clicker Question 9:

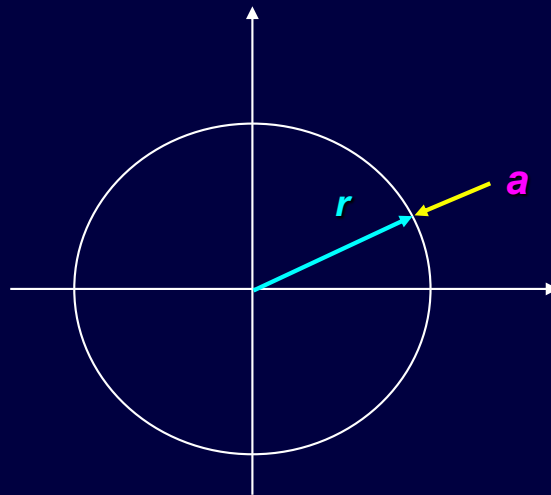
Below we have a car that is circling around some point moving at a constant speed. Is the car accelerating?

- (a) Yes
- (b) No
- (c) Yes, but only part of the time



## Acceleration in UCM:

- UCM results in acceleration:
  - This is called Centripetal Acceleration
  - Direction: (toward center of circle)
  - Magnitude:



$$a_c = \frac{v^2}{r}$$

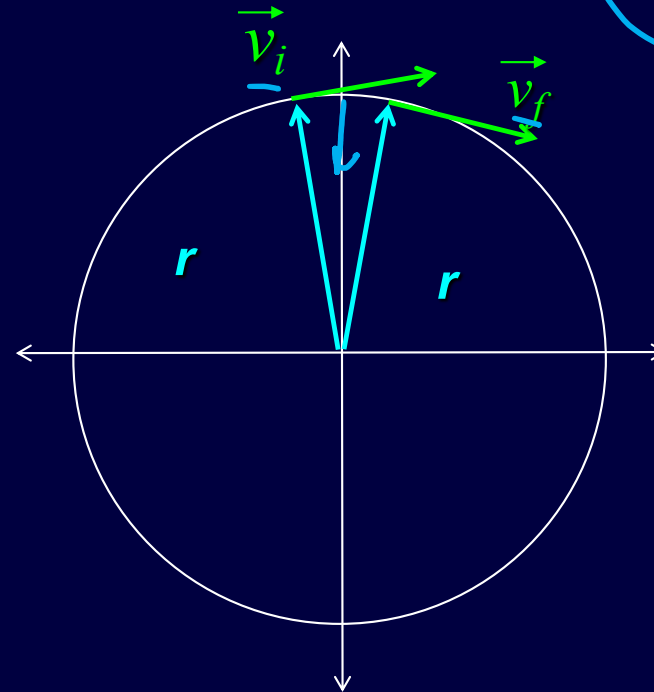
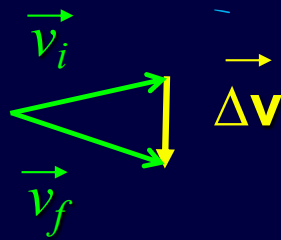
$$= \omega^2 r$$





## Acceleration in UCM:

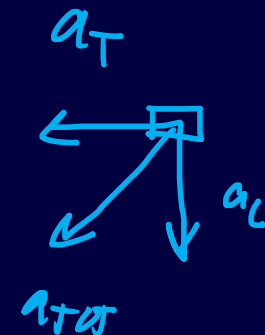
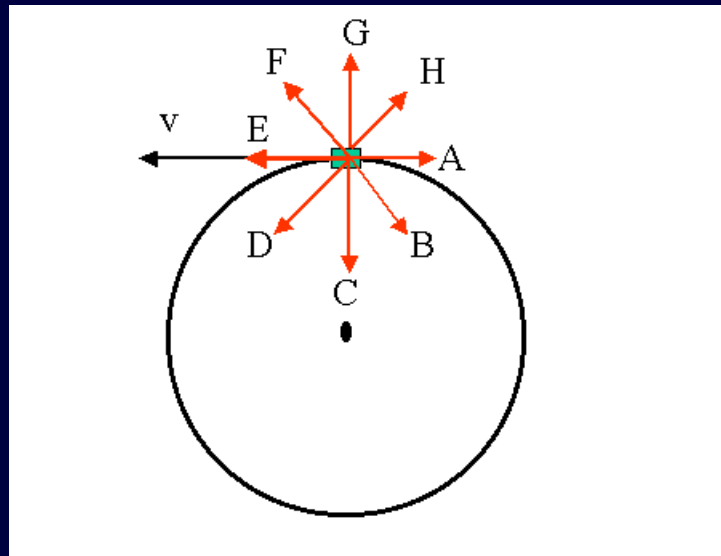
- Consider average acceleration in time  $\Delta t$



- Acceleration is towards the center of the circular path

## Clicker 10:

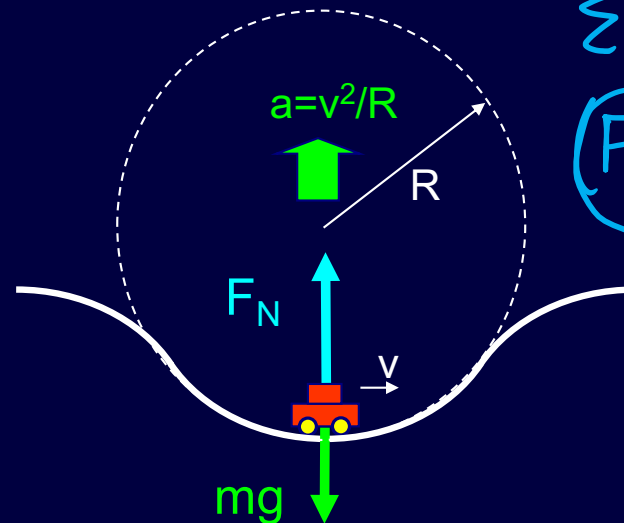
An object is rotating in a circle. As it is rotating its speed is increasing. What direction is its acceleration vector pointing? A, B, C, D, E, F, G, or H



## Clicker Question 11:

Suppose you are driving through a valley whose bottom has a circular shape. If your mass is  $m$ , what is the magnitude of the normal force  $F_N$  exerted on you by the car seat as you drive past the bottom of the hill?

- A.  $F_N < mg$
- B.  $F_N = mg$
- C.  $F_N > mg$



$$\Sigma F_y = ma$$
$$(F_N - mg) = +ma$$